



PILLAI COLLEGE OF ENGINEERING, NEW PANVEL 210422

(Autonomous) (Accredited 'A+' by NAAC)

END SEMESTER EXAMINATION

SECOND HALF 2021(Supplementary)

SEM-I

BRANCH: FE (Mech/Auto/EXTC)

Subject: Engineering Mechanics

Max. Marks: 60

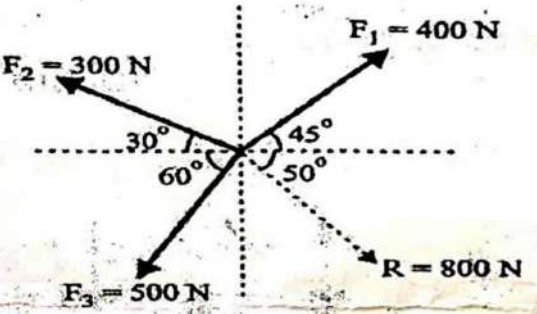
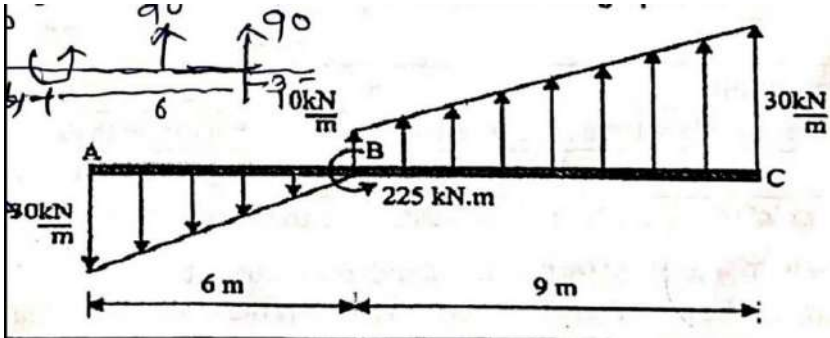
Time: 02.00 Hours

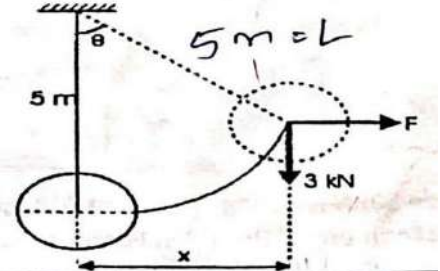
Date: 02-06-2022

N.B 1. Q.1 is compulsory

ME 104, AE 104, ET104

2. Attempt any two from the remaining three questions

Q.1.	Attempt all	Answers
a)	<p>Find Force F4 so as to give the resultant of system of forces as shown .</p> 	<p>F4 = 961.62  <math>\theta = 39.58</math>            4<sup>th</sup> Quadrant  <math>\sum f(x) = +</math>  <math>\sum f(y) = -</math></p>
b)	<p>Members ABC is loaded with Different loads            Find the Magnitude of the Resultant and its locations along Span AC</p> 	<p>R = 90            M = 2070(anti-clock)            X = 23</p>
c)	<p>Determine the magnitude and Directions of the force <math>F=34i+150j-290k</math></p>	<p><math>F = \sqrt{F_x^2 + F_y^2 + F_z^2} = 475</math>  <math>F_x = F \cos \theta_x = \theta_x = 43.42</math>  <math>\theta_y = 71.59</math>  <math>\theta_z = 127.62</math></p>

d)	<p>Determine the horizontal distance 'x' to which a 5m long inextensible string holding a weight 3 kN can be. Pulled before the string breaks. The string can withstand a maximum force 6 kN as shown in fig determine also required force 'F'</p> 	<p>Theorem</p> <p><math>\theta = 60</math>  <math>F = 5.2 \text{ kN}</math>  <math>x = 4.33</math></p>
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Q.2.	Attempt all	Answers	
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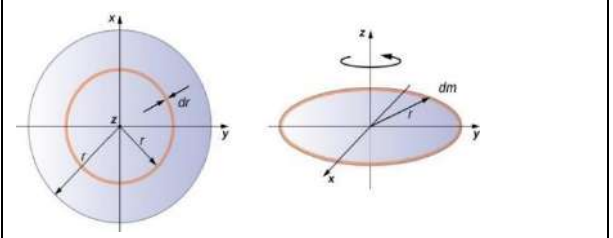
a)	<p>Differentiate between Centre of Gravity (CG) and Centroid With example and also Explain the Moment of inertia with Fig and example.</p>	Centre of Gravity	Centroid
		<p>The point where the total weight of the body focuses upon</p>	<p>It is referred to the geometrical centre of a body</p>
		<p>It is the point where the gravitational force (weight) acts on the body</p>	<p>It is referred to the centre of gravity of uniform density objects</p>
		<p>It is denoted by g</p>	<p>It is denoted by c</p>
		<p>It is a physical behaviour of the object, a point where all the weight of an object is acting</p>	<p>It is a physical behaviour of the object, a point where all the weight of an object is acting</p>

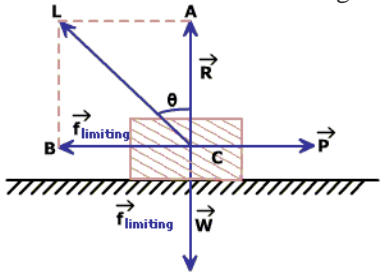
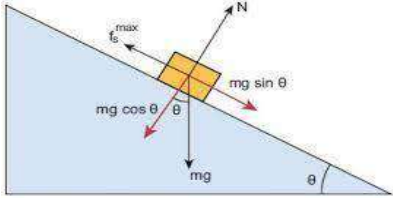
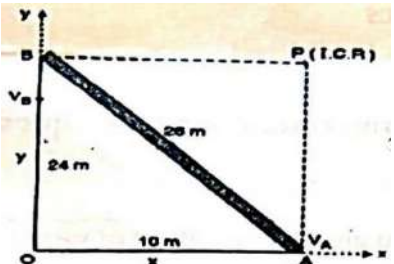
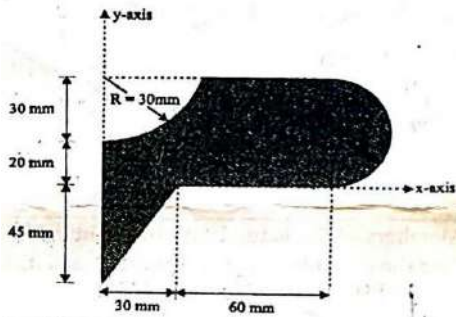
Moment of Inertia is the sum of the product of each point mass and square of its distance from the axis of rotation.

**Example:** Imagine you are on a bus right now. You find a seat and sit down. The bus starts moving forward. After a few minutes, you arrive at a bus stop and the bus stops. What did

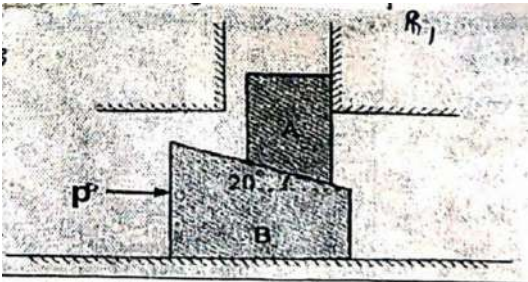
upper body moved forward whereas your lower body did not move. Why is that? It is because of Inertia. Your lower body is in contact with the bus but your upper body is not in contact

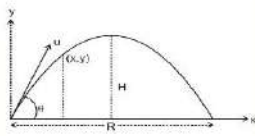
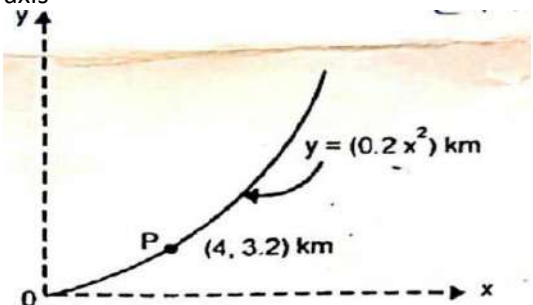
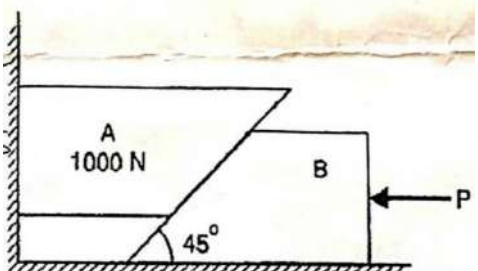
your body stopped with the bus but your upper body kept moving forward, that is, it resisted change in its state.



<p>b)</p>	<p>Define and explain the terms, Angle of Friction and Angle of Repose with Fig and example</p>	<p>Angle of Friction :          Definition : The angle between the resultant of frictional force and the normal reaction makes with the normal force is called the angle of friction.</p>  <p>Angle of friction</p> <p>Angle of Repose:          Definition : Angle of repose is defined as the angle that an inclined plane makes with the horizontal when a body placed on it just starts sliding.</p>  <p>Figure 3.29 Angle of repose</p>
<p>c)</p>	<p>A rod 'AB' 26m long leans against a vertical wall. The end 'A' of the rod is 10mtrs from the wall. Determine the velocity of the end 'B' sliding down vertically and the angular velocity of the rod AB</p> 	<p><math>X = 10 \quad y = 24</math>  <math>L = 26</math>  <math>V_A = 24 \text{ m/sec}</math>  <math>X^2 + Y^2 = C^2</math>  <math>V_B = -10</math>  <math>w = 1 \text{ rad/sec counter clockwise}</math></p>
<p>d)</p>	<p>Locate Centroid of the given Lamina</p> 	<p><math>X = 54.87</math>  <math>Y = 18.45</math></p>

Q3)	Attempt all	
a)	State and explain Lami's theorem and Varignon's theorem with example	<p>Lami's theorem relates the magnitudes of coplanar, concurrent and non-collinear forces that maintain an object in static equilibrium. The theorem is very useful in analyzing most of the mechanical as well as structural systems.</p> <p>Lami's theorem states, "When three forces acting at a point are in equilibrium, then each force is proportional to the sine of the angle between the other two forces".</p> <p>Referring to the above diagram, consider three forces A, B, C acting on a particle of rigid body making angles <math>\alpha</math>, <math>\beta</math> and <math>\gamma</math> with each other.</p> <p>Varignon's theorem states that the sum of the moments produced by any two concurrent forces with respect to a point is equal to the moment produced by the resultant with respect to the same point. This theorem is also known as theorem of moments. The moment produced by R with respect to a moment center O is <math>R \times d</math>. The summation of the moments of F1 and F2 with respect to the same moment center O is <math>F_1 d_1 + F_2 d_2</math>.</p> <p>Then as per Varignon's theorem, <math>R d = F_1 d_1 + F_2 d_2</math></p> <p>(state an example)</p>
b)	Explain velocity, average velocity, acceleration, average acceleration with figure.	<p>Velocity- Velocity is essentially a vector quantity. It is the rate of change of distance. It is the rate of change of displacement. Speed of an object moving can never be negative. The velocity of a moving object can be zero.</p> <p>Average velocity- Average velocity is defined as <b>the change in position or displacement (<math>\Delta x</math>) divided by the time intervals (<math>\Delta t</math>) in which the displacement occurs</b>. The average velocity can be positive or negative depending upon the sign of the displacement. The SI unit of average velocity is meters per second (m/s or <math>\text{ms}^{-1}</math>)</p> <p>Acceleration- In <a href="#">mechanics</a>, <b>acceleration</b> is the <a href="#">rate</a> of change of the <a href="#">velocity</a> of an</p>

		<p>object with respect to time.          Accelerations are <u>vector</u> quantities (in that they have <u>magnitude</u> and <u>direction</u>).          Average Acceleration- Average acceleration refers to <b>the rate at which the velocity changes</b>. We divide the change in velocity by an elapsed time to find out the average acceleration of anything. For instance, if the velocity of a crazy ball increases from 0 to 60 cm/s in 3 seconds, the average acceleration of the ball would be 20 cm/s/s.</p>
<p>c)</p>	<p>A block 'A' supports a load of <math>W=5000\text{N}</math> and is to be raised by forcing Wedge 'B' under it . The angle of friction for all surfaces in contact.          Determine the force <math>P</math> which is necessary to start the wedge under the block .The block &amp; Wedge have negligible weight</p> 	<p>Block A <math>\rightarrow R_2 = 7281.23</math>          Block B <math>\rightarrow R_1 = 6169 \quad \mu = 0.27</math>  <math>\Phi = 15</math>  <math>P = 6003.58</math>  <math>R_3 = 0.595 \times 7281.23 = 4332.33</math></p>
<p>d)</p>	<p>A force of magnitude <math>50\text{KN}</math> is acting at a point <math>A(2,3,4)\text{m}</math> towards point <math>B(6,-2,-3)\text{m}</math> . Find the moment of the given force about a point <math>D(-1,1,2)</math></p>	<p><math>S_a = 3i + 2j + 2k</math>  <math>F = F_1 e_{AB} = 50[4i - 5j - 7k] / \sqrt{4^2 + 5^2 + 7^2}</math>  <math>= 21.08j - 26.35j - 36.89k</math>  <math>M_D = r_{DA} * F = 21.08i + 152.85 - 121.2k</math></p>
<p>Q4.</p>	<p>Attmpt all</p>	
<p>a)</p>	<p>State and explain the Projectile Motion with formula of trajectory.</p>	<p>When a body is thrown with velocity making some angle with horizontal, it follows parabolic trajectory called projectile.          At general time ,velocity of the particle will  <math>v = v \cos \theta i + (v \sin \theta - gt) j</math>  <math>v_x = v \cos \theta</math>  <math>v_y = (v \sin \theta - gt)</math>  <math>X = v \cos \theta t</math>  <math>Y = v \sin \theta t - 2gt^2</math></p>

		<p>Eliminating <math>t, Y = v \sin \theta / v \cos \theta x - (g * x^2) / (2v^2 \cos^2 \theta)</math></p> <p><math>Y = x \tan \theta - (g * x^2) / (2v^2 \cos^2 \theta)</math> is called equation of trajectory.</p>
<p>b)</p>	<p>Derive formulas for max height range and time of flight of projectile motions.</p>	<p>We have  <math>u_x = u \cos \theta, a_x = 0</math>  <math>u_y = u \sin \theta, a_y = -g</math>  <math>S_x = u_x t + \frac{1}{2} a_x t^2</math>  <math>\Rightarrow x = u \cos \theta t + 0 \Rightarrow x = u \cos \theta t \dots (1)</math>  <math>S_y = u_y t + \frac{1}{2} a_y t^2 \Rightarrow y = u \sin \theta t - \frac{1}{2} g t^2</math>  <math>\Rightarrow y = u \sin \theta \left( \frac{x}{u \cos \theta} \right) - \frac{1}{2} g \left( \frac{x}{u \cos \theta} \right)^2</math>  or, <math>y = x \tan \theta - \frac{g x^2}{2u^2 \cos^2 \theta}</math>  <math>\Rightarrow y = x \tan \theta - \frac{g x^2}{2u^2} (1 + \tan^2 \theta)</math>  Thus is path equation of projectile  For time of flight  We have <math>S_y = 0 \Rightarrow 0 = u_y T - \frac{1}{2} g T^2</math>  <math>\Rightarrow 0 = u \sin \theta T - \frac{1}{2} g T^2</math>  <math>\Rightarrow T = \frac{2u \sin \theta}{g}</math>  <math>R = u_x T = u \cos \theta \cdot \frac{2u \sin \theta}{g}</math>  <math>\frac{u^2}{g} \cdot 2 \sin \theta \cos \theta = \frac{u^2 \sin 2\theta}{g}</math>  <math>H = u_y T + \frac{1}{2} a_y T^2</math>  <math>= u \sin \theta \cdot \frac{T}{2} - \frac{1}{2} g \left( \frac{T}{2} \right)^2</math>  <math>= u \sin \theta \cdot \frac{u \sin \theta}{g} - \frac{1}{2} g \left( \frac{u \sin \theta}{g} \right)^2</math> (Since particle will reach at highest after time <math>T/2</math>)  <math>= \frac{u^2 \sin^2 \theta}{g} - \frac{u^2 \sin^2 \theta}{2g}</math>  <math>= \frac{u^2 \sin^2 \theta}{2g}</math></p> 
<p>c)</p>	<p>An airplane travels on a crushed path point 'P'. It has a speed of 360m/hr which is increasing at a rate of 0.5 mtrs/sec<sup>2</sup>. Determine at 'P'.  The Magnitude of total acceleration  Angle made by m acceleration vector with positive x-axis</p> 	<p><math>p = [1 + (dy/dx)^2]^{3/2} = 16.792 \text{ cm}</math>  <math>dy^2/dx^2 = 16792 \text{ m}</math>  <math>dt = 0.5 \text{ m/s}^2</math>  <math>a = 0.777 \text{ m/s}^2</math>  eqn = <math>dy/dx = 0</math>  <math>dy/dx = \phi.6 \quad x = 4</math>  <math>\tan \theta = a_n / dt = 0.595 / 0.5 = \theta = 50</math>  <math>\tan \alpha = dy/dx</math>  <math>\tan \alpha = 1.6</math>  <math>\alpha = 58</math>  <math>\alpha + \theta = 108</math></p>
<p>d)</p>	<p>Block 'A' weighing 100N is to be raised by applying a horizontal force 'P' on another block 'B' of same weight as shown in fig. Calculate the minimum value of 'P' to push block 'A' up the surface take co-efficient of friction = 0.25 at all surfaces.</p> 	<p><math>P = 3536</math>  <math>N_2 = 3233</math>  <math>N_1 = 0.883 * 3233</math>  <math>N_3 = 2714</math></p>